

## What's Going On?

### Checking In

A Handy Trick

### Minds on

Expanding... again!

### Action!

Breaking up is hard to do!

### Consolidation

That Little Guy?

**Learning Goal - I will be able to factor trinomials in the form  $ax^2 + bx + c$ .**

# F.F.M.

It's back!

Factor Fully.

$$4x^2 + 8x - 60$$

$$= 4(x^2 + 2x - 15)$$

$$= 4(x+5)(x-3)$$

Common Factor  
if possible

Find two integers  
that sum to 2  
and multiply to -15.

## Checking In

### What's the Pattern with the Signs?

Second term positive, third term positive

$$\begin{aligned}x^2 + 10x + 25 &= (x+5)(x+5) \\ &= (x+5)^2\end{aligned}$$

Second term negative, third term positive

$$x^2 - 8x + 12 = (x-6)(x-2)$$

Second term positive, third term negative

$$x^2 + x - 6 = (x+3)(x-2)$$

Second term negative, third term negative

$$x^2 - 3x - 10 = (x+2)(x-5)$$

- When the second *and* third terms in the trinomial are positive, we know that our integers are **both positive**.
- When the second term in the trinomial is negative and the third term is positive we know that our integers are **both negative**.
- When the second term in the trinomial is positive and third term is negative, we know that the larger integer will be positive and the smaller integer will be negative.
- When the second *and* third terms in the trinomial are negative, we know that the larger integer will be negative and the smaller integer will be positive.

**Minds on**

# Expanding... Again!

$$(2x + 3)(x + 4)$$

$$(2x + 3)(x + 4) \quad \text{Nothing fancy... just FOIL it!}$$

$$= 2x^2 + 8x + 3x + 12$$

$$= 2x^2 + 11x + 12$$

## Minds on

So...  $(2x + 3)(x + 4)$

when expanded is:  $2x^2 + 11x + 12$

This means that if you were asked to factor  $2x^2 + 11x + 12$ , you *should* end up with  $(2x + 3)(x + 4)$ .

But how would you factor it?

## Minds on

Let's look back at the expansion for a moment...

$$(2x + 3)(x + 4) \\ = 2x^2 + 8x + 3x + 12$$

What if I asked you to factor this 4-termed polynomial?

**Factor by Grouping!**

**Minds on****Factor by Grouping!**

$$\begin{aligned} & (2x^2 + 8x) + (3x + 12) \\ &= 2x(x+4) + 3(x+4) \\ & \quad \underbrace{\hspace{10em}}_{\text{Binomial Common Factors}} \\ &= (x+4)(2x+3) \end{aligned}$$



**Minds on**

$$(2x + 3)(x + 4)$$

$$= 2x^2 + 8x + 3x + 12$$

So we can factor  
from here.

$$= 2x^2 + 11x + 12$$

But we can't seem to  
factor from here.

So the question is, how do we get from the red step to the green step?!

**Action!**

## Breaking Up Is Hard To Do!

$$2x^2 + 11x + 12$$

$$= 2x^2 + 8x + 3x + 12$$

If we can get to here, we can factor by grouping.

$$= 2x(x + 4) + 3(x + 4)$$

$$= (2x + 3)(x + 4)$$

So how did we get from the red step to the green step?

To get to that second step, we **broke up** the  $+11x$  into  $+8x$  and  $+3x$

But how did we know to break it up into  $+8x$  and  $+3x$ ?  
Why not  $+1x$  and  $+10x$  or  $+2x$  and  $+9x$  or  $-52x$  and  $+63x$ ?

**Action!**

## Breaking Up Is Hard To Do!

$$2x^2 + 11x + 12$$

$$= 2x^2 + 8x + 3x + 12$$

To get to that second step, we  
broke up the +11x into +8x and +3x

But how did we know to break it up into +8x and +3x?  
Why not +1x and +10x or +2x and +9x or -52x and +63x?

**We had to find two numbers that added up to 11 (OBVIOUSLY!)**

**and multiplied to give 24! (obviously?)**

## Action!

# Breaking Up Is Hard To Do!

We had to find two numbers that added up to 11 (OBVIOUSLY!)  
and multiplied to give 24! (obviously?)

$$(2x + 3)(x + 4)$$

Look back at the expansion...

$$= (2x)(1x) + (2x)(4) + (3)(1x) + (3)(4)$$

Now take a closer look at the coefficients before we simplified!

$$= (2x)(1x) + (2x)(4) + (3)(1x) + (3)(4)$$

(2, 4, 3, 1)

(2, 1, 3, 4)

All of the coefficients on the First and Last terms appear on the two middle terms!

So if we multiplied the two sets together,  
the products would be **the same!**

**Action!**

## Breaking Up Is Hard To Do?

$$(2x + 3)(x + 4)$$

$$= 2x^2 + 8x + 3x + 12$$

$$8 \times 3 \\ = 24$$

$$2 \times 12 \\ = 24$$

To here...

We need to break up  $11x$  into two terms where the coefficients add to 11 and multiply to give  $2 \times 12 = 24$

$$= 2x^2 + 11x + 12 \longrightarrow \text{So to get from here}$$

## Factoring $ax^2 + bx + c$

To factor trinomials in the form  $ax^2 + bx + c$

1. Always common factor first if possible!
2. Break up the middle term
  - Replace the middle term ( $bx$ ) by two terms whose coefficients have a sum of  $b$  and a product of  $(a \times c)$
3. Factor by grouping
  - Group **pairs** of terms and remove a common factor from each
  - Then common binomial factor

## Factor $6x^2 + 13x - 5$

1. There is no factor common to all three terms.
2. Find two numbers that sum to +13 and multiply to -30 (+6 x -5)

Factors of -30	Sum
+1, -30	-29
-1, +30	+29
+2, -15	-13
-2, +15	+13

We break up  $13x$  into  $-2x$  and  $+15x$

3. Factor  $(6x^2 - 2x) + (15x - 5)$

Factor by grouping

$$= 2x(3x-1) + 5(3x-1)$$

Binomial common factor

$$= (3x-1)(2x+5)$$

## Factor $6x^2 - 13x + 6$

1. There is no factor common to all three terms.
2. Find two numbers that sum to -13 and multiply to 36 (+6 x +6)

*\*We know both are negative*

Factors of 36	Sum
-1, -36	-37
-2, -18	-20
-3, -12	-15
-4, -9	-13

We break up -13x into -4x and -9x

3. Factor  $(6x^2 - 4x) - (9x + 6)$

$$= 2x(3x-2) + 3(-3x+2)$$

*Factor out*

$$= 2x(3x-2) - 3(3x-2)$$

$$= (3x-2)(2x-3)$$

*BCF*



## Factoring $ax^2 + bxy + cy$

To factor trinomials in the form  $ax^2 + bx + c$

1. Always common factor first if possible!
2. Break up the middle term
  - Replace the middle term ( $bxy$ ) by two terms whose coefficients have a sum of  $b$  and a product of  $a \times c$ .
3. Factor by grouping
  - Group **pairs** of terms and remove a common factor from each
  - Then common binomial factor

## Consolidation

That little guy?  
I wouldn't worry about that little guy.

Factor  $4x^2 - 5xy - 6y^2$ .

## Consolidation

Homework

**WRITE IN YOUR LOG**

**Pg. 163**

**1-5 (a, d, f)**

**AND 4(n, o, r)**

**5(h, i)**

### Challenge Problem

Prove that if a trinomial in the form  $ax^2 + bx + c$

( $a \neq 1$ ) can be factored into a product of two binomials the middle term can be broken up into two terms where the coefficients sum to  $b$  and multiply to  $(a \times c)$ .