

MFM2P – Equations of Lines – Day 7: Determining Slope from Two Points

You can determine the slope of a line given any two points that lie on that line.

Given two points:

1. Label the points 1 and 2.
 - the x-coordinate of Point 1 is x_1
 - the y-coordinate of Point 1 is y_1
 - the x-coordinate of Point 2 is x_2
 - the y-coordinate of Point 2 is y_2
2. Label each x-coordinate and y-coordinate properly.

3. Plug the values into the equation:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

4. Simplify the numerator (this is your rise)
5. Simplify the denominator (this is your run)
6. Reduce your fraction to lowest terms.

Example

Find the slope of the line through the points $(3, 4)$ and $(5, 2)$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{2 - 4}{5 - 3}$$

$$= \frac{-2}{2}$$

$$= -1$$

$$\therefore \text{The slope is } -1$$

Determine the slope of the line through the given points.

$$A(0, 3) \quad B(2, 0)$$

$$m = \frac{0-3}{2-0}$$

$$= \frac{-3}{2}$$

$$C(-2, 0) \quad D(0, 5)$$

$$m = \frac{5-0}{0-(-2)}$$

$$= \frac{5}{2}$$

if you subtract
a negative...
ADD

$$E(2, 3) \quad F(5, 0)$$

$$m = \frac{0-3}{5-2}$$

$$= \frac{-3}{3}$$

$$= -1$$

$$G(2, 1) \quad H(3, 6)$$

$$m = \frac{6-1}{3-2}$$

$$= \frac{5}{1}$$

$$= 5$$

$$I(-3, -3) \quad J(-3, 7)$$

$$m = \frac{7-(-3)}{-3-(-3)}$$

$$\rightarrow 7+3$$

$$\rightarrow -3+3$$

$$= \frac{10}{0}$$

$$= \text{undefined}$$

$$K(-2, 1) \quad L(3, 5)$$

$$m = \frac{5-1}{3-2}$$

$$= \frac{4}{1}$$

$$\rightarrow 3+2$$

$$M(25, 30) \quad N(35, 20)$$

$$m = \frac{20-30}{35-25}$$

$$= \frac{-10}{10}$$

$$= -1$$

$$O(-13, -23) \quad P(31, 17)$$

$$m = \frac{17-(-23)}{31-(-13)}$$

$$\rightarrow 17+23$$

$$\rightarrow 31+13$$

$$= \frac{40}{44}$$

$$= \frac{10}{11}$$

$$\text{lowest terms}$$

$$Q(-200, -100) \quad R(30, -6)$$

$$m = \frac{-6-(-100)}{30-(-200)}$$

$$\rightarrow -6+100$$

$$\rightarrow 30+200$$

$$= \frac{94}{230}$$

$$= \frac{47}{115}$$

$$\text{lowest terms}$$

$$S(-12, -15) \quad T(-20, -4)$$

$$m = \frac{-4-(-15)}{-20-(-12)}$$

$$\rightarrow -4+15$$

$$\rightarrow -20+12$$

$$= \frac{11}{-8}$$

$$= -\frac{11}{8}$$

$$\text{put the negative sign on top (rise)}$$