

What's Going On?

Checking In

Minds on

Graphing From a TOV

Action!

Graphing $y = x^2$

Consolidation

First and Second Differences

Learning Goal - I will understand how to graph quadratic functions in the form $y = ax^2$.

Minds on

Graphing from a TOV

What's a TOV?

A TOV is a Table of Values

(x, y)

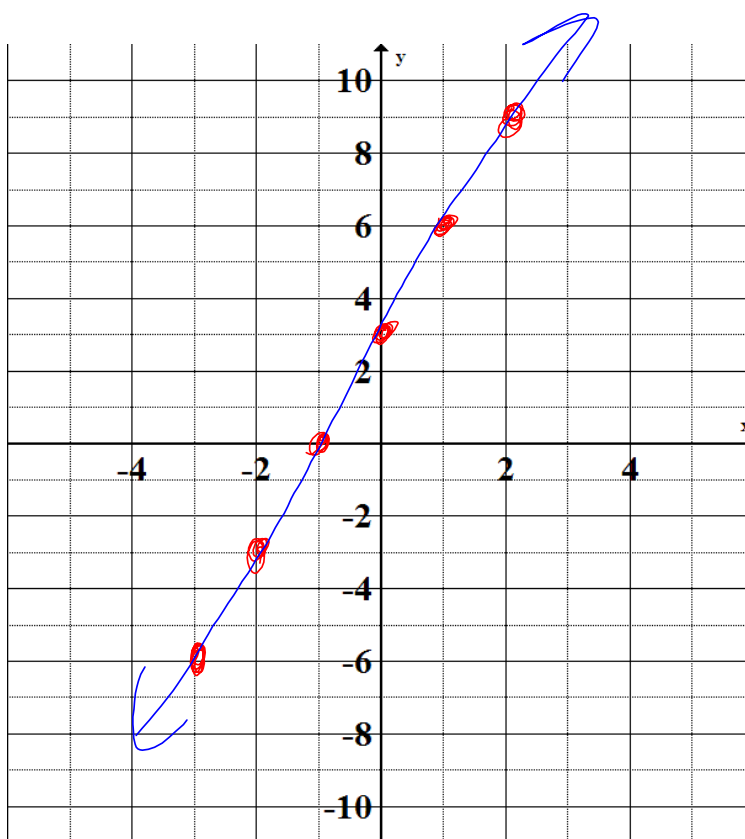
Basically it is a list of ordered pairs (points on a graph) for some function.

To graph, given a TOV, we just plot the points!

Minds on

Graphing from a TOV

| X | Y |
|----|----|
| -3 | -6 |
| -2 | -3 |
| -1 | 0 |
| 0 | 3 |
| 1 | 6 |
| 2 | 9 |



Action!

Graphing $y = x^2$

If you were asked to graph the function $y = x^2$, using a table of values, how would you do it?

| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| 1 | 1 |
| 2 | 4 |
| 3 | 9 |

Before we even do that, does anyone remember what kind of graph this will be?

parabola

First, start with some values for x !

I usually go with -3, -2, -1, 0, 1, 2...

$$(-3)(-3) = +9$$

Action!

Graphing $y = x^2$

If you were asked to graph the function $y = x^2$, using a table of values, how would you do it?

| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |

Now, find the value of y that goes with each x -value!

To do that, plug the x -value into the equation!

Action!Graphing $y = x^2$ **Notice the y -values!**

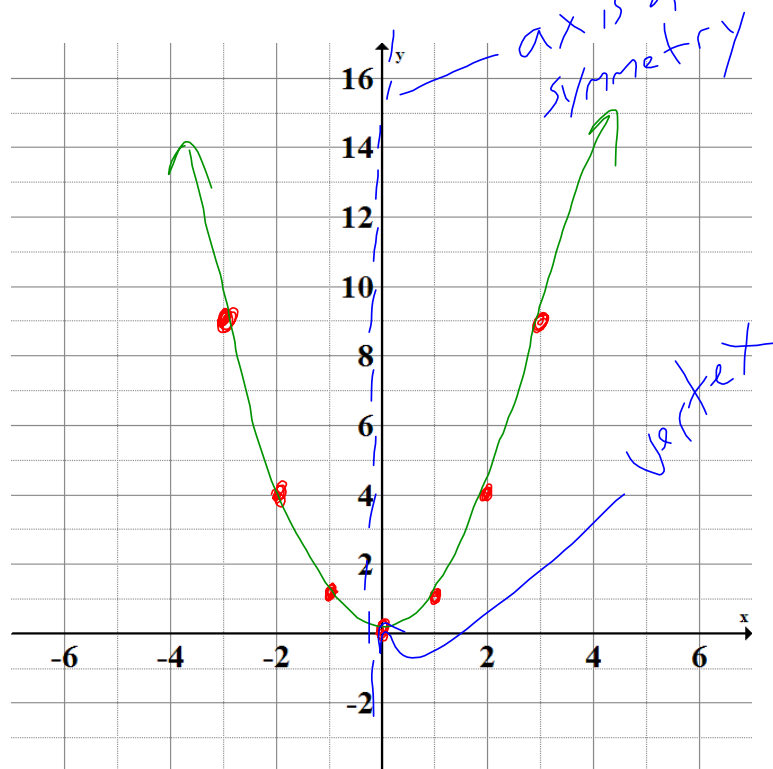
| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |

Action!

Graphing $y = x^2$

Now, just plot the points!

| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |



Action!

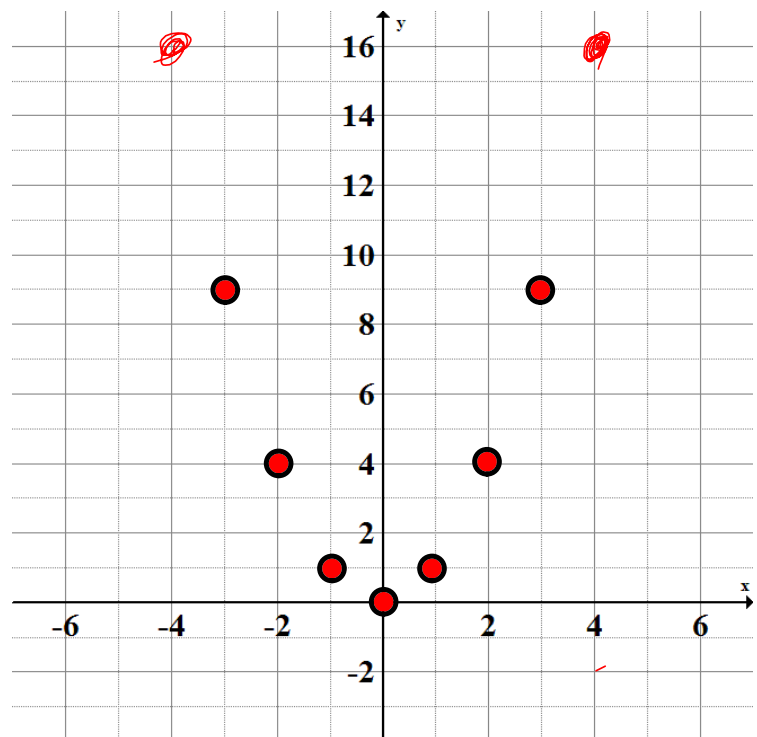
Graphing $y = x^2$

Once you have plotted the points, try and see if you can figure out a pattern among them.

(What would the next points be?)

$$4^2 =$$

| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |

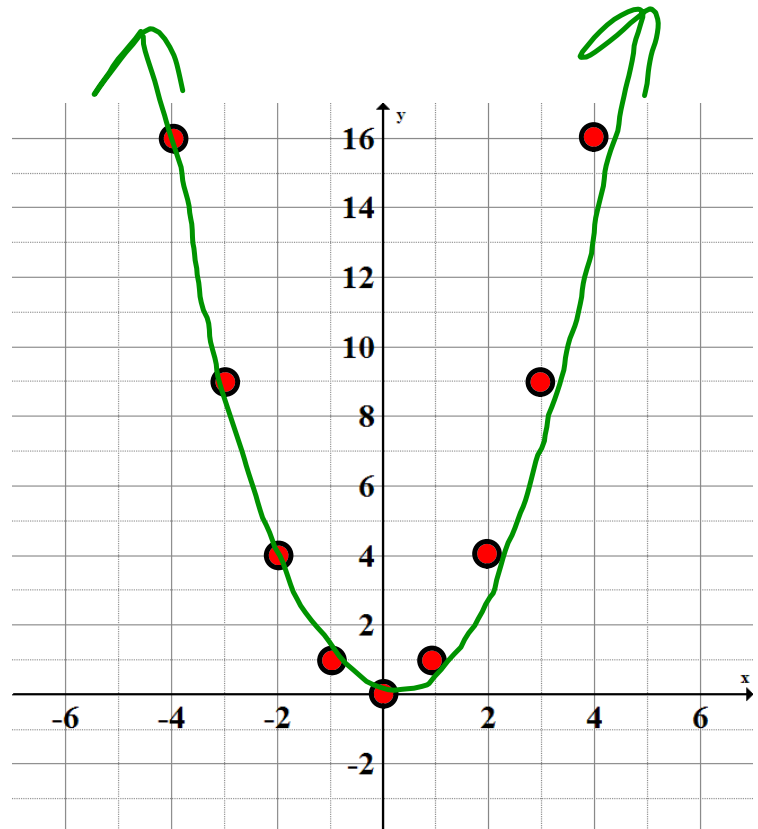


Action!

Graphing $y = x^2$

Now draw a curve through your points!

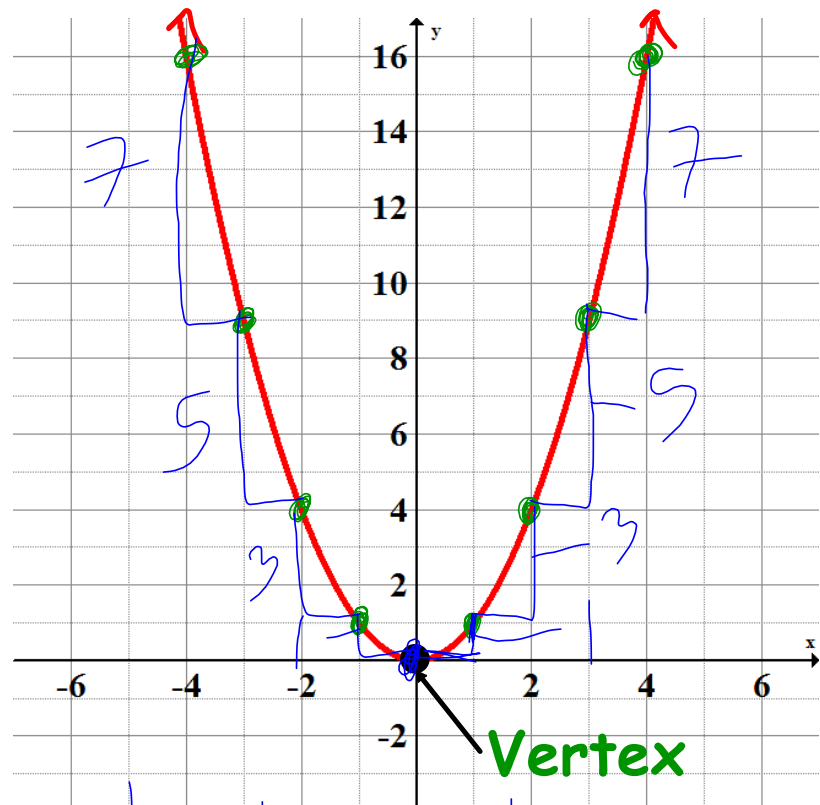
| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |



Action!Graphing $y = x^2$ - **Step Pattern**

Table of Values?

| x | y |
|-----|-----|
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |



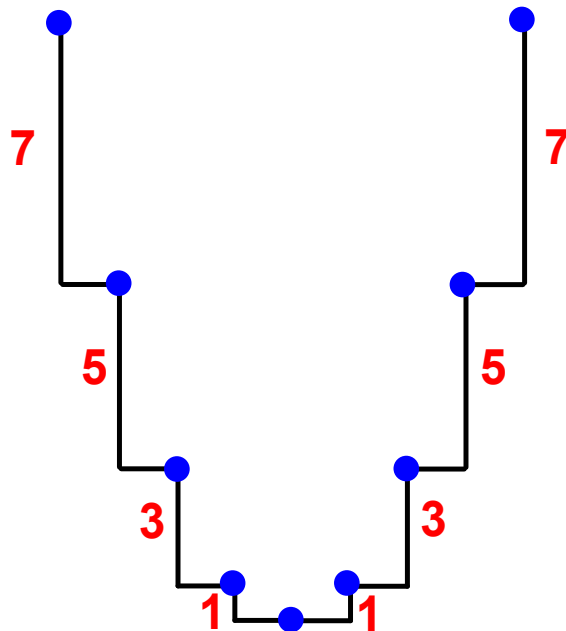
The general step pattern
is 1, 3, 5, 7, ...

Action!

Graphing $y = x^2$ - Step Pattern

Table of Values?

| x | y |
|-----|-----|
| -4 | 16 |
| -3 | 9 |
| -2 | 4 |
| -1 | 1 |
| 0 | 0 |
| +1 | 1 |
| +2 | 4 |
| +3 | 9 |
| +4 | 16 |

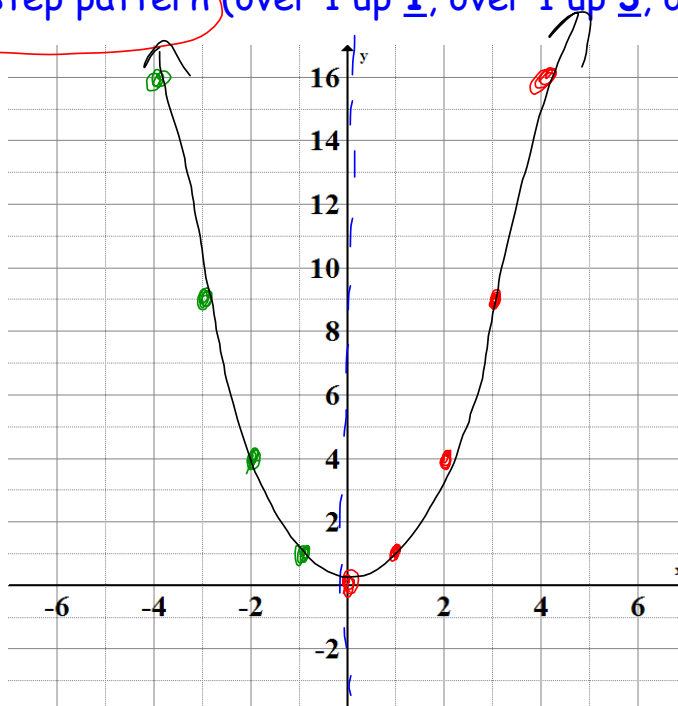


Action!

Graphing $y = x^2$

To graph the function $y = x^2$, plot the **vertex** at (0, 0).

Then use the **step pattern** (over 1 up 1, over 1 up 3, over 1 up 5, etc...)



Consolidation

First and Second Differences

$$y = x^2$$

To calculate first differences, subtract consecutive y-values.

Specifically, subtract a given y-value *from* the *next* y-value.
($y_2 - y_1$)

| x | y | First Differences | Second Differences |
|----|---|-------------------|--------------------|
| -3 | 9 | -5 | |
| -2 | 4 | -3 | +2 |
| -1 | 1 | -1 | +2 |
| 0 | 0 | +1 | +2 |
| 1 | 1 | +3 | +2 |
| 2 | 4 | | |

Consolidation

First and Second Differences

$$y = x^2$$

The first differences give us the step pattern!

Notice that the second differences are **constant**.

| x | y | First Differences | Second Differences |
|----|---|-------------------|--------------------|
| -3 | | | |
| -2 | | | |
| -1 | | | |
| 0 | | | |
| 1 | | | |
| 2 | | | |

Consolidation

Summary

If the first differences in a table of values are equal, the

equation forms a straight line.

If the second differences in a table of values are equal

(and not 0) the equation forms a parabola.

Consolidation

Your turn!

I will give each of you a quadratic equation.

Complete the table of values, then graph your function!

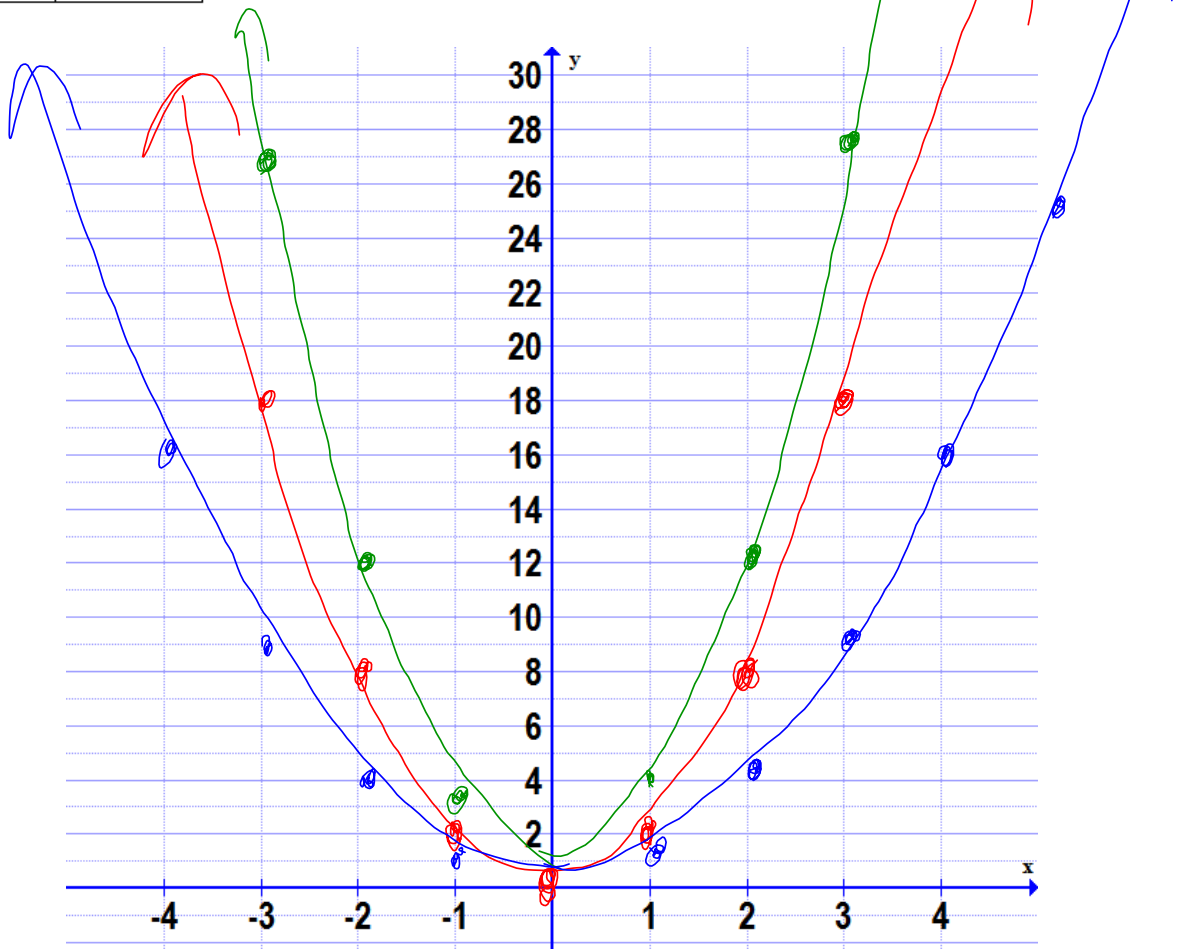
| X | Y | First Differences | Second Differences |
|----|----|-------------------|--------------------|
| -3 | 18 | | |
| -2 | 8 | | |
| -1 | 2 | | |
| 0 | 0 | | |
| 1 | 2 | | |
| 2 | 8 | | |

$$Y = 2x^2$$

$$(1)$$

$$Y = 3x^2$$

$$Y = x^2$$



| x | y | | |
|----------|----------|--------------------------|---------------------------|
| -3 | | First Differences | Second Differences |
| -2 | | | |
| -1 | | | |
| 0 | | | |
| 1 | | | |
| 2 | | | |

