

What's Going On?

Checking In

Minds on

Properties of sin and cos

Action!

Desmos Investigation!

Consolidation

Coordinates of a Point

Learning Goal - I will investigate, and understand, the properties of sinusoidal functions.

Minds on

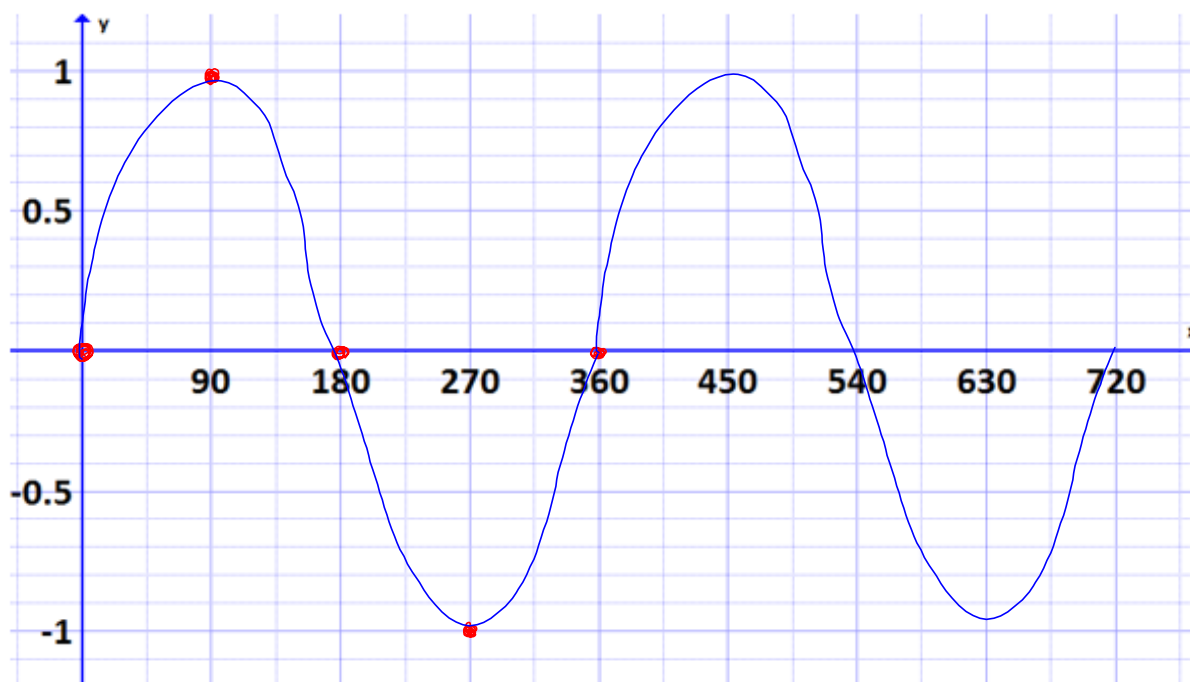
Sinusoidal Functions

A sinusoidal function is a periodic function whose graph looks like smooth symmetrical waves, where any portion of the wave can be horizontally translated onto another portion of the curve; graphs of sinusoidal functions can be created by transforming the graph of the function $y = \sin x$ or $y = \cos x$.

Minds on

Properties of $\sin(\theta)$ and $\cos(\theta)$

$$f(x) = \sin x$$



- The period is 360°

- The equation of the axis is $y = 0$

- The amplitude is 1

The max value is 1

The min value is -1

- The domain is $\{x \in \mathbb{R}\}$

- The range is $\{-1 \leq y \leq 1\}$

- The zeroes are located at $0, 180, 360, \dots$

Minds on

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- The domain is $\{x \in \mathbb{R}\}$
- The range is $\{-1 \leq y \leq 1\}$
- The zeroes are located at $90^\circ, 270^\circ, 450^\circ, \dots$

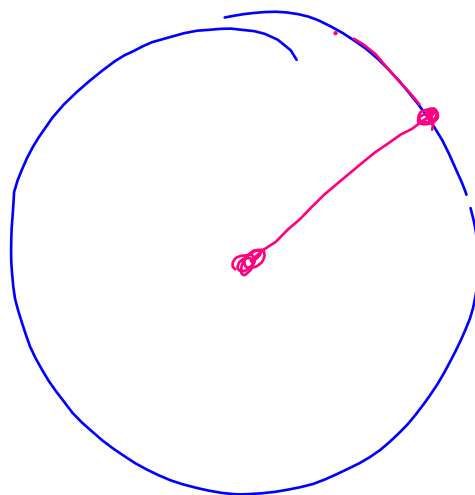
Action!

Desmos Investigation

$$C = 2\pi r$$

$$2(180)$$

$$360(r)$$



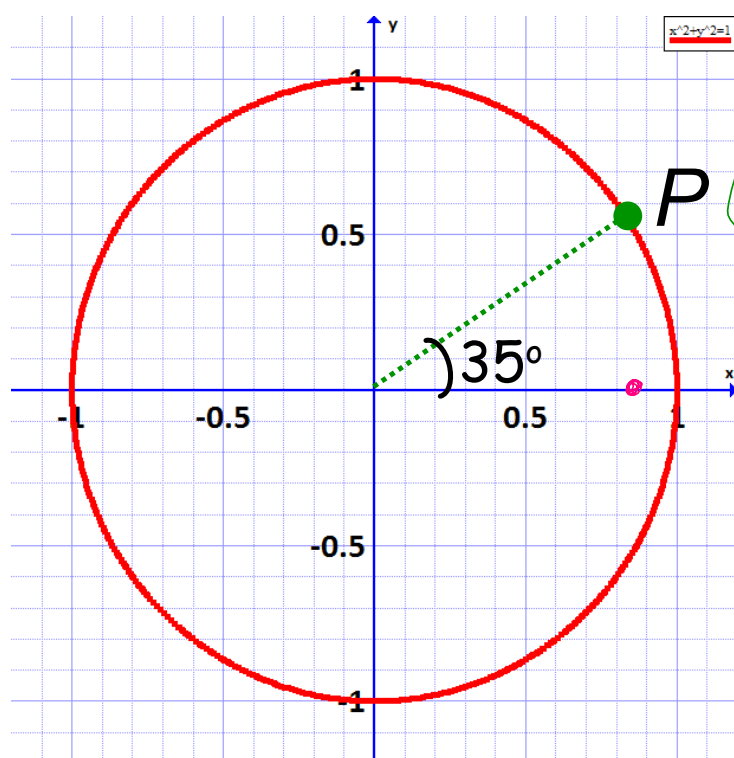
$$\frac{3\pi}{2}$$

$$1.5(180)$$

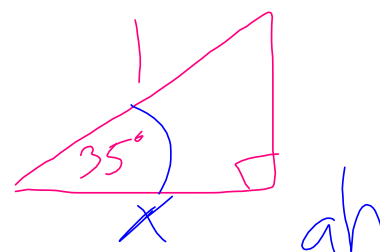
Consolidation

Coordinates of a Point

Determine the exact coordinates of the given point $P(x, y)$.



$$P(\cos 35^\circ, \sin 35^\circ)$$
$$(0.819, 0.573)$$

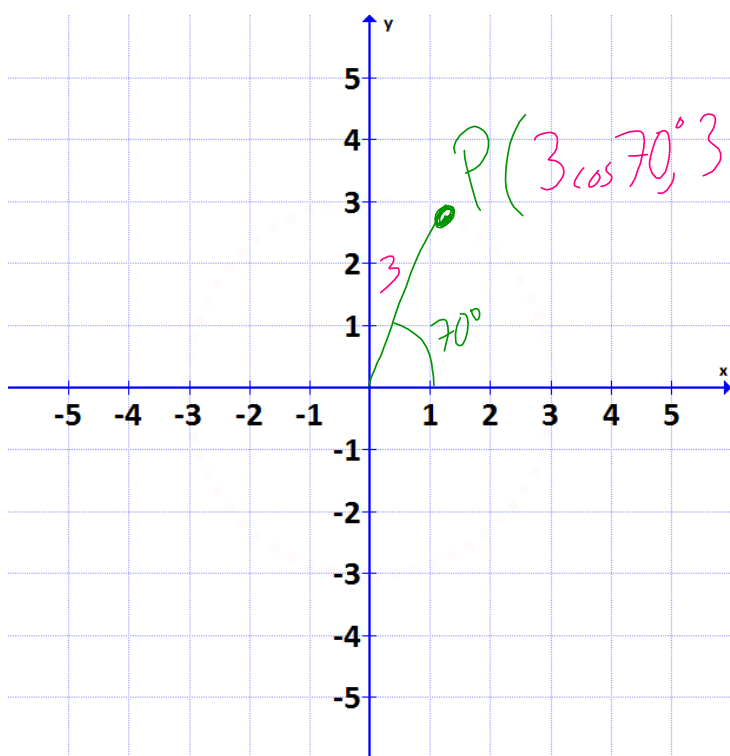


$$\cos 35^\circ = \frac{x}{1}$$

Consolidation

Coordinates of a Point

Determine the coordinates of the point $P(x, y)$ resulting from a rotation of 70 degrees centred at the origin and starting from the point $(3, 0)$.



$$\cos 70^\circ = \frac{x}{3}$$

$$x = 3 \cos 70^\circ$$

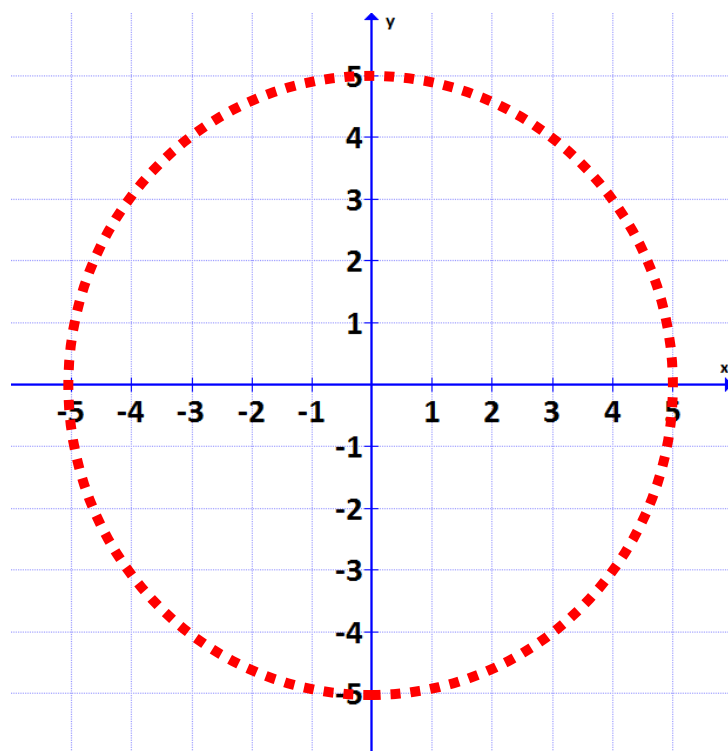
$$\sin 70^\circ = \frac{y}{3}$$

$$y = 3 \sin 70^\circ$$

Consolidation

Coordinates of a Point

Any point $P(x, y)$ on a circle centred at $(0,0)$ with radius r and rotated through an angle θ can be expressed as an ordered pair $(r \cos \theta, r \sin \theta)$.



Find the coordinates of each point.

