

## What's Going On?

**Checking In**

**Minds on**

sin or cos?

**Action!**

Modelling Sinusoidal Functions

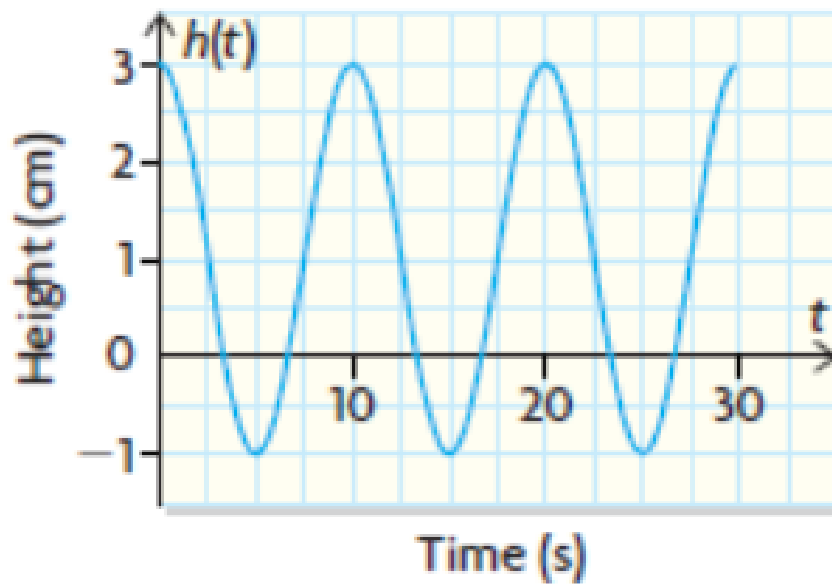
**Consolidation**

Another Ferris Wheel!

**Learning Goal - I will be able to model sinusoidal functions.**

Minds on

sin or cos?



**Action!**

# Modelling

Determine an equation for the following graph:

$$a = 2$$

$$k = 36$$

$$d = 0$$

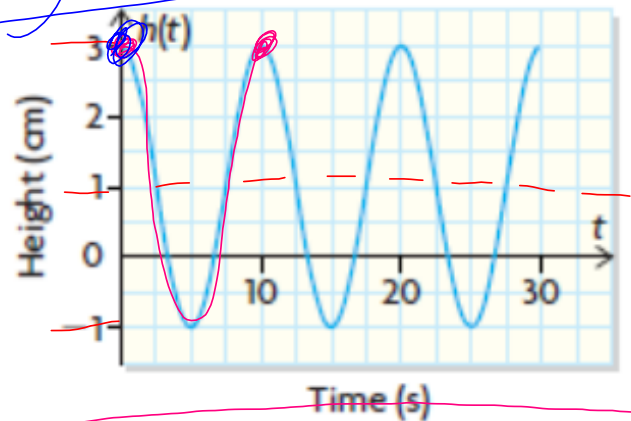
$$c = 1$$

using cos

$$\text{period} = \frac{360}{|k|}$$

$$10 = \frac{360}{k}$$

$$k = 36$$



$$h = a \cos(k(t-d)) + c$$

$$h = 2 \cos(36t) + 1$$

Is there another equation that could be used?

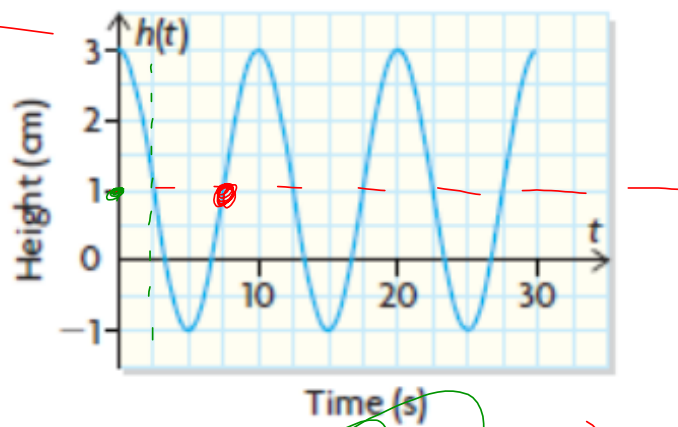
Use sin!

$$a = 2$$

$$k = 36$$

$$d = 7.5$$

$$c = 1$$



$$h = 2 \sin(36(t - 7.5)) + 1$$

$$h = 2 \sin(36t - 270) + 1$$

$$h = 2 \cos(36t) + 1$$

Hector says that the equation is actually  $h(t) = -2 \sin[36t - 90] + 1$ , but  
 Briana says that the equation should be  $h(t) = -2 \cos[36(t - 5)] + 1$ . Who  
 is correct? **Explain.**

Hector

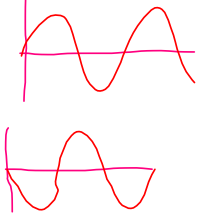
$a = -2$

$k = 36$

$d = 2.5$

$c = 1$

$k(x-d)$



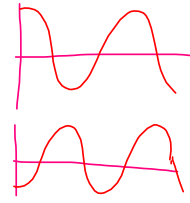
Briana

$a = -2$

$k = 36$

$d = 5$

$c = 1$



We can always change the sign of our a-value (flip about x-axis) and then change the d value (horizontal shift) to end up with equivalent curves in terms of sin and/or cos.

A sinusoidal function has an amplitude of 2 units, a period of  $180^\circ$ , and a maximum at  $(0, 3)$ . Represent the function with an equation in two different ways.

$$a = 2$$

$$k = 2$$

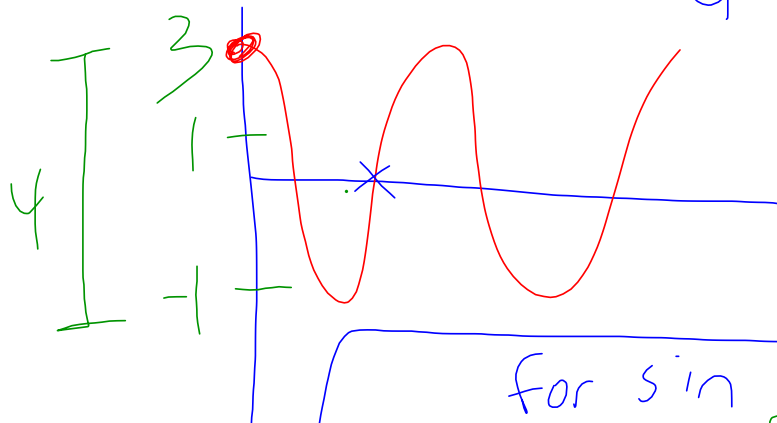
$$d = 0$$

$$c = 1$$

$$y = 2 \cos(2x) + 1$$

↳ one sin

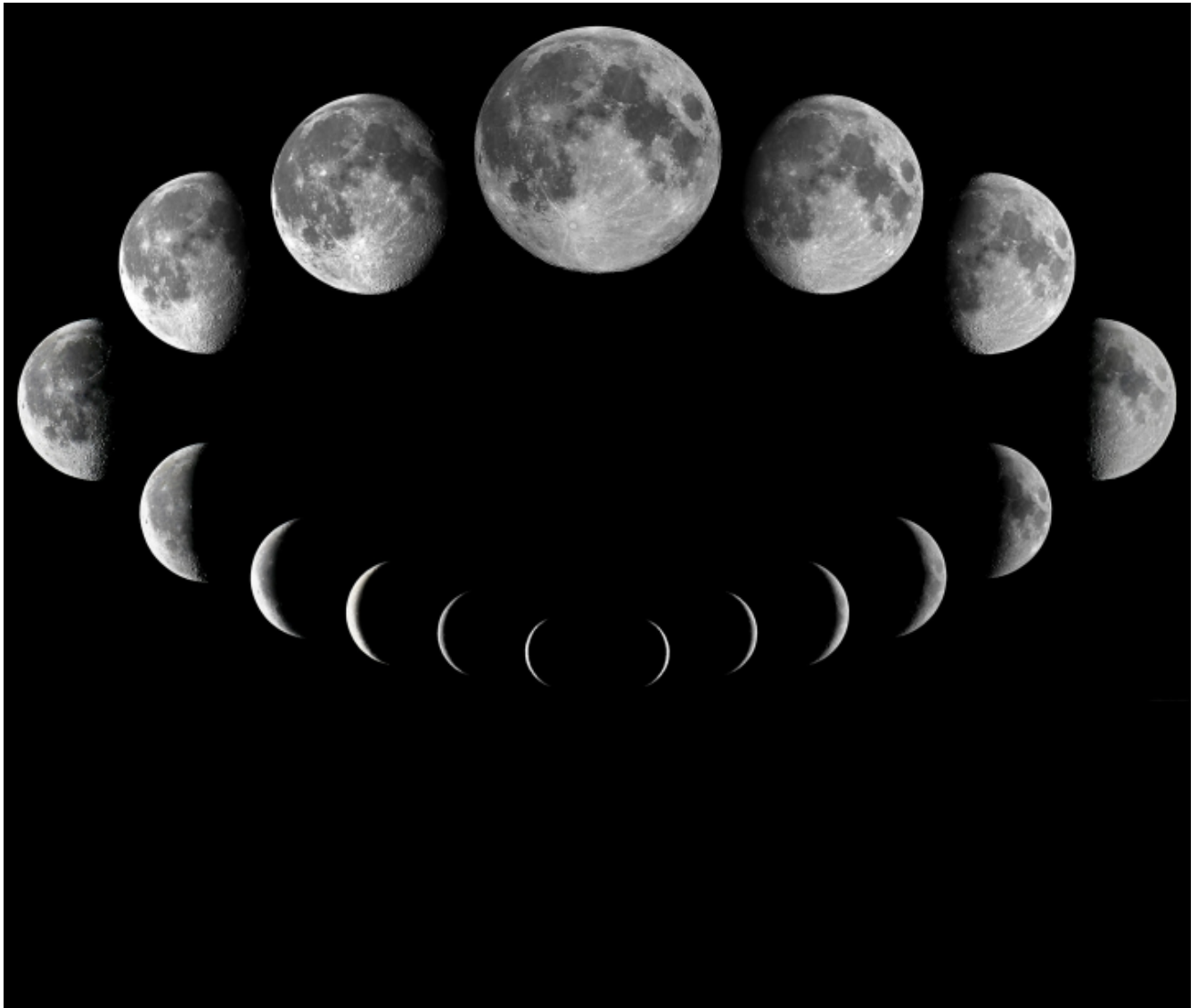
↳ one cos



for sin  
\* or  $-270$

$$y = 2 \sin(2x + 90) + 1$$

$$y = 2 \sin(2(x + 45)) + 1$$



# Phases of the Moon

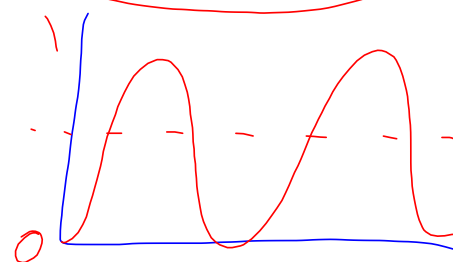


1. Create a function to model the phases of the moon for an entire year. *USE COS*

$$a = -0.5 \quad d = 0$$

$$k = 12 \left( \frac{360}{30} \right)$$

$$c = 0.5$$



$$P = -0.5 \cos(12d) + 0.5$$

2. What is the period of your function?

What significance does it have in terms of our calendar?

$$\frac{360}{12} = 30!$$

*days in a month*

3. List the dates when the moon is full.



## Consolidation

# Another Ferris Wheel!

Mahew is riding a Ferris wheel at a constant speed of 10 km/h. The boarding height for the wheel is 1 m, and the wheel has a radius of 7 m. What is the equation of the function that describes Mahew's height in terms of  $t$ , assuming Mahew starts at the highest point on the wheel?