

What's Going On?

Checking In

Minds on

Rate of Change Recap

Action!

Rate of Change of Polynomial Functions

Consolidation

Instantaneous RoC from Graph

Learning Goal - I will be able to calculate average and instantaneous rates of change for polynomial functions.

Minds on

Secant Lines and Tangent Lines

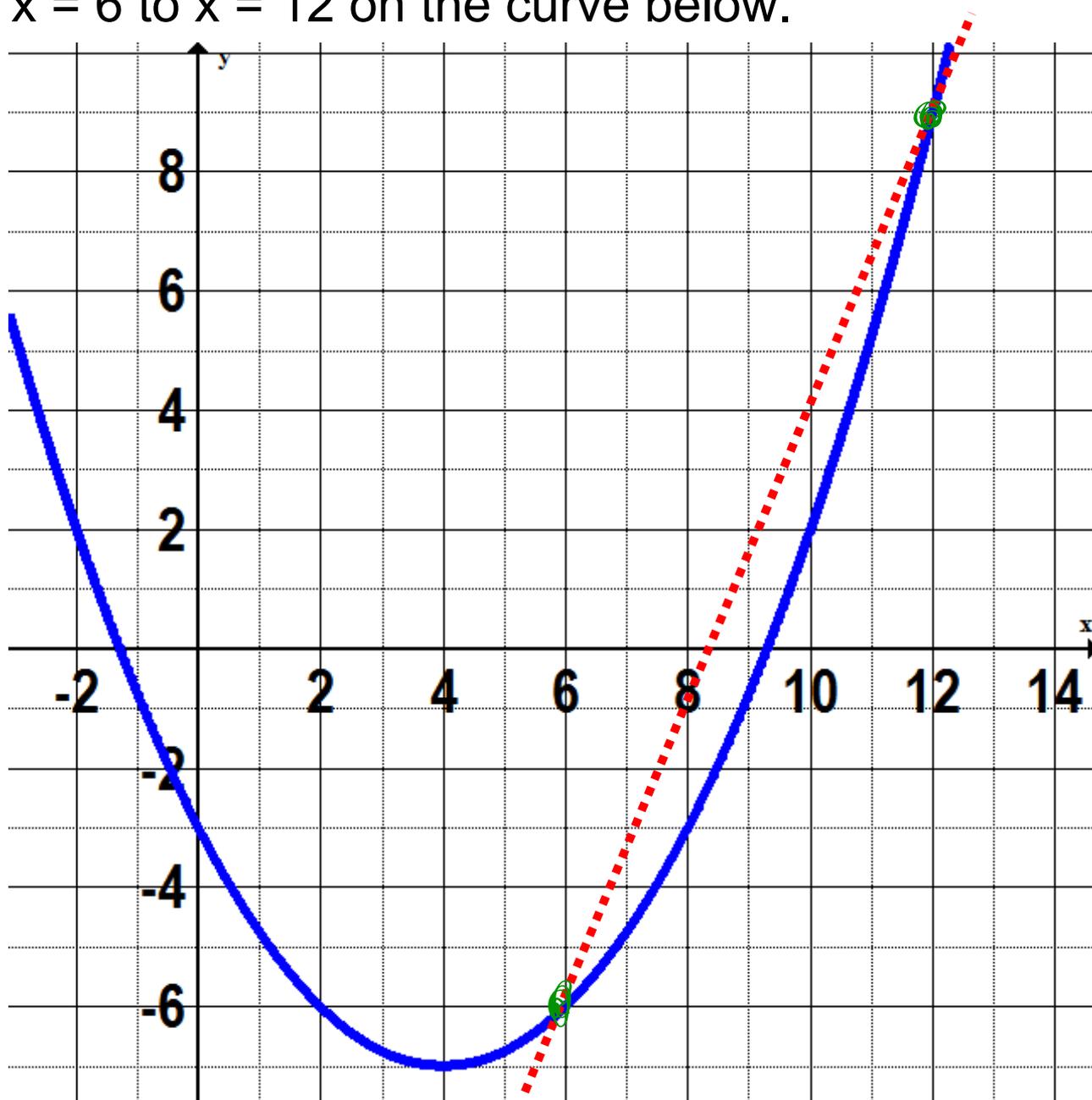
Recall from earlier in the course:

To determine the average rate of change over an interval, we find the slope of a secant line that passes through two points of a curve.

Minds on

Secant Lines and Tangent Lines

Determine the average rate of change from $x = 6$ to $x = 12$ on the curve below.



Average Rate of Change

$$= \frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

$$= \frac{9 - (-6)}{12 - 6}$$

$$= \frac{15}{6} = 2.5$$

Action!

Determining Rate of Change

Average Rate of Change

To determine the average rate of change through two points x_1 and x_2 , use the formula

$$\frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

Action!

Determining Rate of Change

Average Rate of Change

Determine the average rate of change from $x = 2$ to $x = 5$ on the function

$$f(x) = (x - 3)^3 - 1$$

$$\begin{aligned} \text{AOC} &= \frac{f(5) - f(2)}{5 - 2} \\ &= \frac{((5 - 3)^3 - 1) - ((2 - 3)^3 - 1)}{3} \\ &= \frac{(7) - (-2)}{3} \\ &= 3 \end{aligned}$$

Minds on

Secant Lines and Tangent Lines

Recall from earlier in the course:

To determine the instantaneous rate of change at a point, we find the slope of a **secant line** that passes through two very close points of a curve.

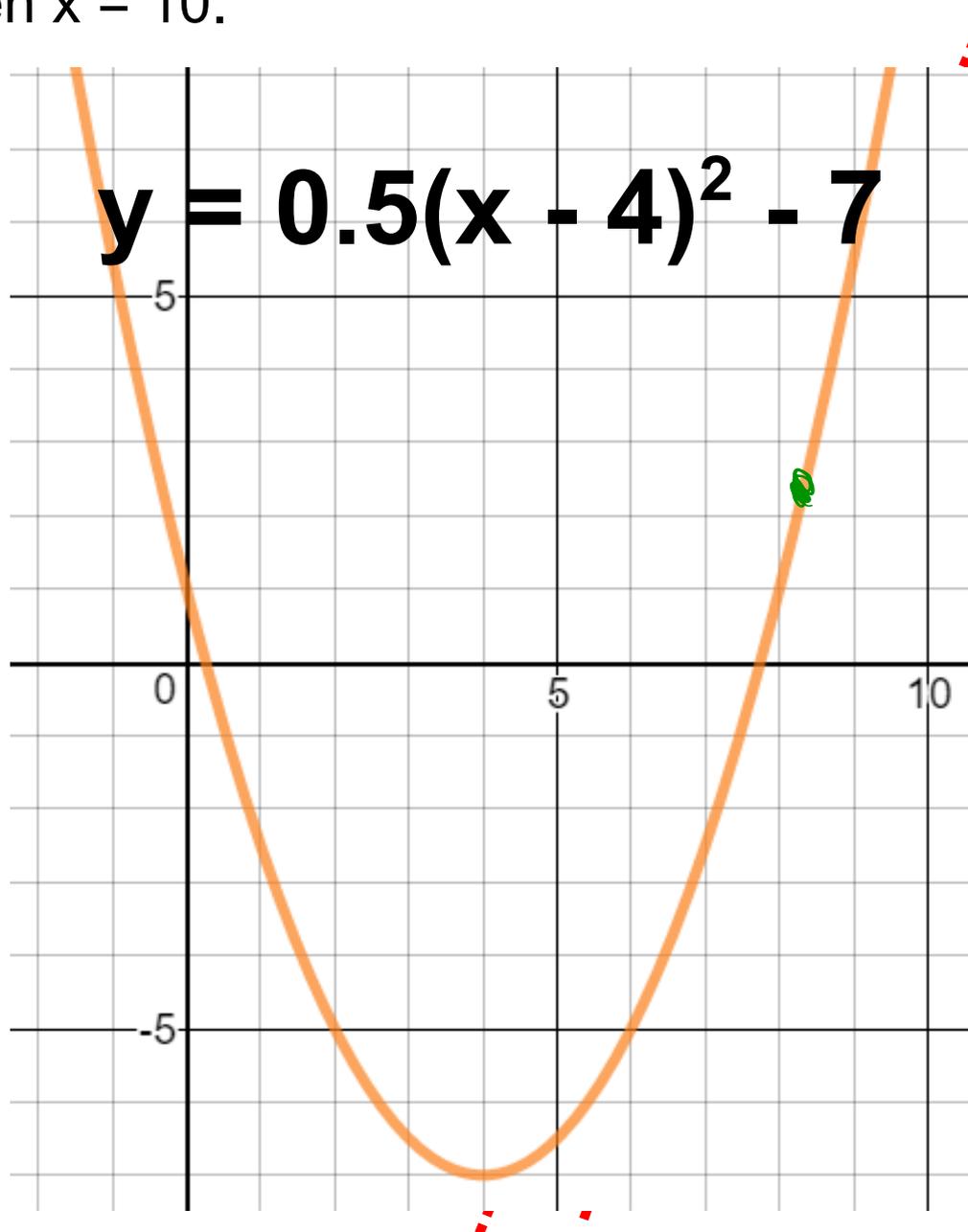
Ideally, this line would pass through our point and no other points on the curve.

This would be called a **tangent line.**

Minds on

Secant Lines and Tangent Lines

Determine the instantaneous rate of change when $x = 10$.



$$\text{r.o.c.} = \frac{f(x+h) - f(x)}{h}$$

where $h = 0.001$

$$= \frac{f(10.001) - f(10)}{0.001}$$

$$= \frac{(0.5(10.001-4)^2 - 7) - (0.5(10-4)^2 - 7)}{0.001}$$

$$= \frac{11.006 - 11}{0.001}$$

$$= 6$$

Action!

Determining Rate of Change

Instantaneous Rate of Change

To determine the instantaneous rate of change of a function when $x = a$ use the difference quotient

$$\frac{f(a + h) - f(a)}{h}$$

where h is a very small number.

0.001

Action!

Determining Rate of Change

Instantaneous Rate of Change

Determine the instantaneous rate of change when $x = 4$ on the function

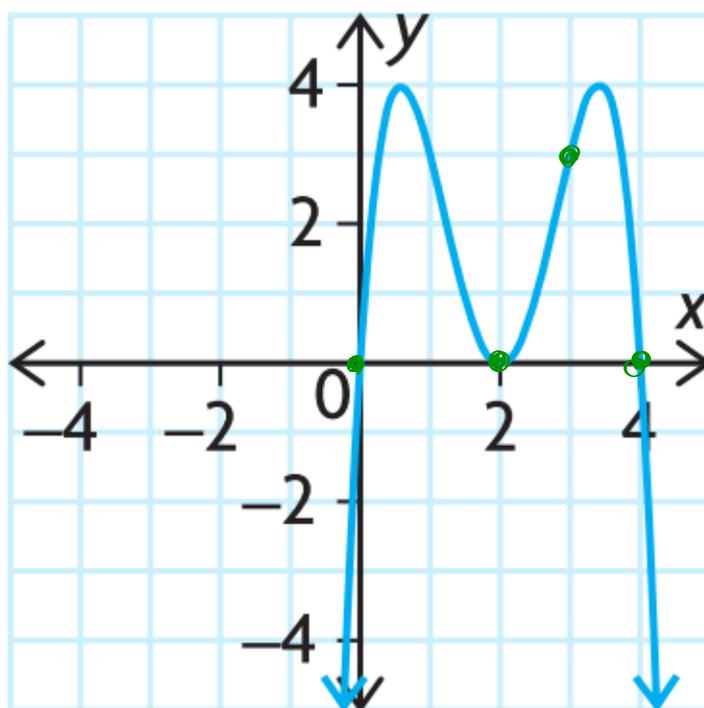
$$f(x) = (x - 3)^3 - 1$$

$$\begin{aligned} \text{r.o.c.} &= \frac{f(4.001) - f(4)}{0.001} \\ &= \frac{((4.001 - 3)^3 - 1) - ((4 - 3)^3 - 1)}{0.001} \\ &= \frac{0.003 - 0}{0.001} \\ &= 3 \end{aligned}$$

Action!

Determining Rate of Change

Given the graph below, estimate the instantaneous rate of change at the point $(3, 3)$.



$$y = ax(x-2)^2(x-4)$$

solve for a!

$$f(3) = a(3)(3-2)^2(3-4)$$

$$3 = a(3)(1)(-1)$$

$$3 = -3a$$

$$a = -1$$

$$y = -x(x-2)^2(x-4)$$

$$\text{roc} = \frac{f(a+h) - f(a)}{h}$$

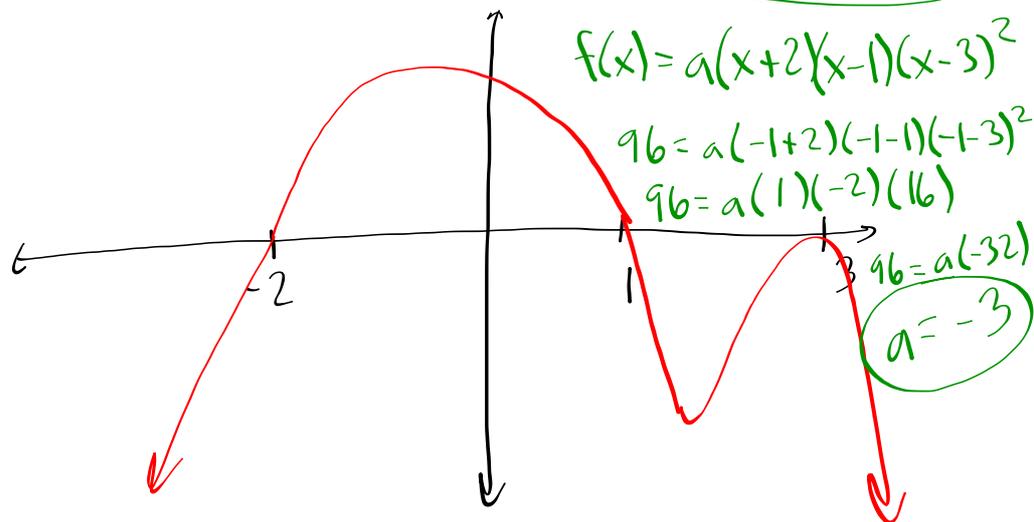
$$= \frac{(-3.001(3.001-2)^2(3.001-4)) - 3}{0.001}$$

$$= \frac{0.004}{0.001}$$

$$= 4$$

Pg. 226 #10

Determine an expression for $f(x)$ in which $f(x)$ is a quartic function, $f(x) > 0$ when $-2 < x < 1$, $f(x) \leq 0$ when $x < -2$ or $x > 1$, $f(x)$ has a double root when $x = 3$, and $f(-1) = 96$.



$$e) (x - 3)(x + 1) + (x - 3)(x + 2) \geq 0$$

$$x^2 - 2x - 3 + x^2 - x - 6 \geq 0$$

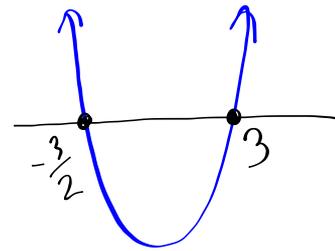
$$2x^2 - 3x - 9 \geq 0$$

$$2x^2 - 6x + 3x - 9 \geq 0$$

$$2x(x - 3) + 3(x - 3) \geq 0$$

$$(x - 3)(2x + 3) \geq 0$$

$$(x - 3)(2x + 3) \geq 0 \text{ when } x \leq -\frac{3}{2} \text{ and } x \geq 3$$



Consolidation

Practice Questions

Pg. 235

1, 3, 8, 11