

Solutions

1.) a) $C = b^a$ b) $M = \frac{2^k}{5}$

2.) a) $x = \log_5 Y$ b) $x = \log_{\frac{4}{1052}} X$

3.) a) 7 b) -3 c) 0 d) -2

4.) a) $\log_9(7 \cdot 49) = 3$ b) $\log_3\left(\frac{54 \cdot 3}{2}\right) = 4$ c) $\log_3 \sqrt{3} = \frac{1}{2}$

5.) a) 2 b) 2

Part B

1.) a) $1 = \log_2\left(\frac{x+4}{x+8}\right)$
 $x = -4$ b) $\log_2\left(\frac{30x}{5}\right) = \log_2 12$
 $x = 2$

2.) ~~a) 3.8~~ ~~b) 7~~ a) 7.9 times stronger

3.) a) 3.8 b) 10^{-21}

4.) 26.5

5.) 33

Part C

1.) $\log_4(6x+4) = b + \log_4(x-1)$

$$b = \log_4\left(\frac{6x+4}{x-1}\right)$$

$$4^b = \frac{6x+4}{x-1}$$

$$4069x - 4069 = 6x + 4$$

$$\frac{4063x}{4063} = \frac{4073}{4063}$$

$$x = 1.0025$$

$$\begin{aligned}
 2.) \quad 70 &= 10 \log \frac{I}{10^{-12}} \\
 7 &= \log I - \log 10^{-12} \\
 7 &= \log I + 12 \\
 -5 &= \log I \\
 10^{-5} &= I \\
 I &= 10^{-5}
 \end{aligned}$$

Therefore, the intensity of sound of the second car is

$$0.00002$$

$$20 = 10 \log \frac{0.00002}{10^{-12}}$$

$$2 = \log 20000000$$

$$x = 73 \text{ dB}$$

$$\begin{aligned}
 3.) \quad a) \quad C &= P(1.038)^t \\
 b) \quad C &= 400(1.038)^{10} \\
 C &= 580.80 \\
 c) \quad 47.95 &= P(1.038)^{10} \\
 47.95 &= P(1.45) \\
 P &= 33.07
 \end{aligned}$$

Part D

$$1.) \quad y = a(K[\log x - d]) + C$$

Vertically compressed by a factor of 5

$$y = \frac{1}{5}(K[\log x - d]) + C$$

Reflected in the Y-axis

$$y = -\frac{1}{5}(K[\log x - d]) + C$$

Horizontally stretched by factor 3

$$y = -\frac{1}{5}\left(\frac{1}{3}[\log x - d]\right) + C$$

Vertically translated 1 unit up

$$y = -\frac{1}{5}\left(\frac{1}{3}[\log x - d]\right) + 1$$

Translated so that the vertical asymptote is $x = -6$

$$y = \frac{1}{5}\left(\frac{1}{3}[\log x + 6]\right) + 1$$